Solutions to Self-Test Problems

CHAPTER 2

ST-1

a. EBIT $5,000,000
   Interest 1,000,000
   EBT $4,000,000
   Taxes (40%) 1,600,000
   Net income $2,400,000

b. NCF = NI + DEP and AMORT
   = $2,400,000 + $1,000,000 = $3,400,000

c. NOPAT = EBIT(1 − T)
   = $5,000,000(0.6)
   = $3,000,000

d. NOWC = Operating current assets − Operating current liabilities
   = (Cash + Accounts receivable + Inventory) − (Accounts payable + Accruals)
   = $14,000,000 − $4,000,000
   = $10,000,000

Total net operating capital = NOWC + Operating long-term assets
   = $10,000,000 + $15,000,000
   = $25,000,000

e. FCF = NOPAT − Net investment in operating capital
   = $3,000,000 − ($25,000,000 − $24,000,000)
   = $2,000,000

f. EVA = EBIT(1 − T) − (Total capital)(After-tax cost of capital)
   = $5,000,000(0.6) − ($25,000,000)(0.10)
   = $3,000,000 − $2,500,000 = $500,000
CHAPTER 3

ST-1 Argent paid $2 in dividends and retained $2 per share. Since total retained earnings rose by $12 million, there must be 6 million shares outstanding. With a book value of $40 per share, total common equity must be $40(6 million) = $240 million. Since Argent has $120 million of debt, its debt ratio must be 33.3%:

\[
\frac{\text{Debt}}{\text{Assets}} = \frac{\text{Debt}}{\text{Debt} + \text{Equity}} = \frac{\$120\text{ million}}{\$120\text{ million} + \$240\text{ million}} = 0.333 = 33.3\%
\]

ST-2 a. In answering questions such as this, always begin by writing down the relevant definitional equations and then start filling in numbers. Note that the extra zeros indicating millions have been deleted in the calculations below.

1. **DSO**

   \[
   \text{DSO} = \frac{\text{Accounts receivable}}{\text{Sales} / 365}
   \]

   \[40.55 = \frac{\text{AR}}{\text{Sales} / 365}\]

   \[\text{AR} = 40.55(2.7397) = 111.1\text{ million}\]

2. **Quick ratio**

   \[
   \text{Quick ratio} = \frac{\text{Current assets} - \text{Inventories}}{\text{Current liabilities}} = 2.0
   \]

   \[= \frac{\text{Cash and marketable securities} + \text{AR}}{\text{Current liabilities}} = 2.0\]

   \[2.0 = \frac{\$100.0 + 111.1}{\text{Current liabilities}}\]

   \[\text{Current liabilities} = (\$100.0 + 111.1)/2 = 105.5\text{ million}\]

3. **Current ratio**

   \[
   \text{Current ratio} = \frac{\text{Current assets}}{\text{Current liabilities}} = 3.0
   \]

   \[= \frac{\text{Current assets}}{\$105.5} = 3.0\]

   \[\text{Current assets} = 3.0(105.5) = 316.50\text{ million}\]

4. **Total assets**

   \[= \text{Current assets} + \text{Fixed assets}\]

   \[= 316.5 + 283.5 = 600\text{ million}\]

5. **ROA**

   \[
   \text{ROA} = \text{Profit margin} \times \text{Total assets turnover}
   \]

   \[= \frac{\text{Net income}}{\text{Sales}} \times \frac{\text{Sales}}{\text{Total assets}}\]

   \[= \frac{\$50}{\$1,000} \times \frac{\$1,000}{\$600}\]

   \[= 0.05 \times 1.667 = 0.083333 = 8.3333\%\]
(6) \[ \text{ROE} = \text{ROA} \times \frac{\text{Assets}}{\text{Equity}} \]

\[ 12.0\% = 8.3333\% \times \frac{\$600}{\text{Equity}} \]

\[ \text{Equity} = \frac{(8.3333\%) \times (\$600)}{12.0\%} \]

\[ = \$416.67 \text{ million} \]

(7) \[ \text{Total assets} = \text{Total claims} = \$600 \text{ million} \]

\[ \text{Current liabilities} + \text{Long-term debt} + \text{Equity} = \$600 \text{ million} \]

\[ \$105.5 + \text{Long-term debt} + \$416.67 = \$600 \text{ million} \]

\[ \text{Long-term debt} = \$600 - \$105.5 - \$416.67 = \$77.83 \text{ million} \]

Note: We could also have found equity as follows:

\[ \text{ROE} = \frac{\text{Net income}}{\text{Equity}} \]

\[ 12.0\% = \frac{\$50}{\text{Equity}} \]

\[ \text{Equity} = \frac{\$50}{0.12} \]

\[ = \$416.67 \text{ million} \]

Then we could have gone on to find long-term debt.

b. Jacobus’s average sales per day were $1,000/365 = $2.7397 million. Its DSO was 40.55, so accounts receivable equal 40.55($2.7397) = $111.1 million. Its new DSO of 30.4 would cause AR = 30.4($2.7397) = $83.3 million. The reduction in receivables would be $111.1 – $83.3 = $27.8 million, which would equal the amount of cash generated.

(1) \[ \text{New equity} = \text{Old equity} - \text{Stock bought back} \]

\[ = \$416.7 - \$27.8 \]

\[ = \$388.9 \text{ million} \]

Thus,

\[ \text{New ROE} = \frac{\text{Net income}}{\text{New equity}} \]

\[ = \frac{\$50}{\$388.9} \]

\[ = 12.86\% \text{ (versus old ROE of 12.0\%)} \]

(2) \[ \text{New ROA} = \frac{\text{Net income}}{\text{Total assets} - \text{Reduction in AR}} \]

\[ = \frac{\$50}{\$600 - \$27.8} \]

\[ = 8.74\% \text{ (versus old ROA of 8.33\%)} \]
The old debt is the same as the new debt:

\[
\text{Debt} = \text{Total claims} - \text{Equity} = $600 - $416.7 = $183.3 \text{ million}
\]

New total assets = Old total assets - Reduction in AR

\[
= $600 - $27.8 = $572.2 \text{ million}
\]

Therefore,

\[
\frac{\text{Debt}}{\text{Old total assets}} = \frac{$183.3}{$600} = 30.6\%
\]

while

\[
\frac{\text{New debt}}{\text{New total assets}} = \frac{$183.3}{$572.2} = 32.0\%
\]

**Chapter 4**

**ST-1**

a. 0 8% 1 2 3 4

\[
\text{FV} = ?
\]

$1,000 is being compounded for 3 years, so your balance at Year 4 is $1,259.71:

\[
FV_N = PV(1 + I)^N = $1,000(1 + 0.08)^3 = $1,259.71
\]

Alternatively, using a financial calculator, input N = 3, I/YR = 8, PV = -1000, and PMT = 0; then solve for FV = $1,259.71.

b. 0 2% 4 8 12 16

\[
\text{FV} = ?
\]

There are 12 compounding periods from Quarter 4 to Quarter 16.

\[
FV_N = PV \left( 1 + \frac{I_{\text{NOM}}}{M} \right)^{NM} = FV_{12} = $1,000(1.02)^{12} = $1,268.24
\]

Alternatively, using a financial calculator, input N = 12, I/YR = 2, PV = -1000, and PMT = 0; then solve for FV = $1,268.24.

c. 0 8% 1 2 3 4

\[
\text{FV} = ?
\]

\[
FVA_4 = 250 \left[ (1 + 0.08)^4 \frac{1 - 0.08}{0.08} \right] = $1,126.53
\]

Using a financial calculator, input N = 4, I/YR = 8, PV = 0, and PMT = -250; then solve for FV = $1,126.53.
d. 

\[
\begin{array}{cccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
\hline
\end{array}
\]

\[
PMT \left[ \frac{(1 + 0.08)^4}{0.08} - \frac{1}{0.08} \right] = 1,259.71
\]

\[
PMT(4.5061) = 1,259.71
\]

\[
PMT = 279.56
\]

Using a financial calculator, input \( N = 4 \), I/YR = 8, PV = 0, and FV = 1259.71; then solve for PMT = −$279.56.

### ST-2

a. Set up a time line like the one in the preceding problem:

\[
\begin{array}{cccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
\hline
PV = ? & ? & ? & ? & 1,000 \\
\end{array}
\]

Note that your deposit will grow for 3 years at 8%. The deposit at Year 1 is the PV, and the FV is $1,000. Here is the solution:

\[
N = 3, \quad I/YR = 8, \quad PMT = 0, \quad FV = 1000; \quad then \ PV = 793.83.
\]

Alternatively,

\[
PV = \frac{FV_N}{(1 + I)^N} = \frac{1,000}{(1 + 0.08)^3} = 793.83
\]

b. 

\[
\begin{array}{cccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
\hline
\end{array}
\]

Here we are dealing with a 4-year annuity whose first payment occurs 1 year from today and whose future value must equal $1,000. Here is the solution: \( N = 4 \), I/YR = 8; PV = 0; FV = 1000; then PMT = $221.92. Alternatively,

\[
PMT \left[ \frac{(1 + 0.08)^4}{0.08} - \frac{1}{0.08} \right] = 1,000
\]

\[
PMT(4.5061) = 1,000
\]

\[
PMT = 222.92
\]

c. This problem can be approached in several ways. Perhaps the simplest is to ask this question: “If I received $750 1 year from now and deposited it to earn 8%, would I have the required $1,000 4 years from now?” The answer is “no”:

\[
\begin{array}{cccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
\hline
\end{array}
\]

\[
FV_3 = 750(1.08)(1.08)(1.08) = 944.78
\]

This indicates that you should let your father make the payments rather than accept the lump sum of $750.
You could also compare the $750 with the PV of the payments:

\[
\begin{array}{ccccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
221.92 & 221.92 & 221.92 & 221.92 \\
\end{array}
\]

\( N = 4, \quad I = 8\% \), \( PMT = -221.92, \quad FV = 0 \); then \( PV = $735.03 \).

Alternatively,

\[
PVA = \frac{1}{0.08} - \frac{1}{(0.08)(1 + 0.08)^4} = $735.03
\]

This is less than the $750 lump sum offer, so your initial reaction might be to accept the lump sum of $750. However, it would be a mistake to do so. The problem is that, when you found the $735.03 PV of the annuity, you were finding the value of the annuity today. You were comparing $735.03 today with the lump sum of $750 in 1 year. This is, of course, invalid. What you should have done was take the $735.03, recognize that this is the PV of an annuity as of today, multiply $735.03 by 1.08 to get $793.83, and compare this $793.83 with the lump sum of $750. You would then take your father’s offer to make the payments rather than take the lump sum 1 year from now.

d.  
\[
\begin{array}{ccccccc}
0 & 1 = ? & 1 & 2 & 3 & 4 \\
-750 & & & & 1,000 \\
\end{array}
\]

\( N = 3, \quad PV = -750, \quad PMT = 0, \quad FV = 1000; \) then \( I = 10.0642\% \).

e.  
\[
\begin{array}{ccccccc}
0 & 1 = ? & 1 & 2 & 3 & 4 \\
186.29 & 186.29 & 186.29 & 186.29 \\
\end{array}
\]

\( FV = 1,000 \)

\( N = 4, \quad PV = 0, \quad PMT = -186.29, \quad FV = 1000; \) then \( I = 19.9997\% \).

You might be able to find a borrower willing to offer you a 20% interest rate, but there would be some risk involved—he or she might not actually pay you your $1,000!

f.  
\[
\begin{array}{ccccccc}
0 & 8\% & 1 & 2 & 3 & 4 \\
400 & ? & ? & ? \\
\end{array}
\]

\( FV = 1,000 \)

Find the future value of the original $400 deposit:

\[
FV_6 = PV(1 + 1)^6 = 400(1 + 0.04)^6 = $400(1.2653) = $506.12.
\]

This means that, at Year 4, you need an additional sum of $493.88: $1,000.00 - $506.12 = $493.88. This amount will be accumulated by making 6 equal payments that earn 8% compounded semiannually, or 4% each 6 months: \( N = 6, \quad I = 4, \quad PV = 0, \quad FV = 493.88; \) then \( PMT = $74.46 \). Alternatively,
PMT \left( \frac{(1 + 0.04)^6 - 1}{0.04} \right) = 493.88

PMT(6.6330) = 493.88

PMT = 74.46

g. 
EFF% = \left( 1 + \frac{\text{INOM}}{M} \right)^M - 1.0

= \left( 1 + \frac{0.08}{2} \right)^2 - 1.0

= 1.0816 - 1 = 0.0816 = 8.16%

**ST-3** Bank A’s effective annual rate is 8.24%:

EFF% = \left( 1 + \frac{0.08}{4} \right)^4 - 1.0

= 1.0824 - 1 = 0.0824 = 8.24%

Now Bank B must have the same effective annual rate:

\left( 1 + \frac{1}{12} \right)^{12} - 1.0 = 0.0824

\left( 1 + \frac{1}{12} \right)^{12} = 1.0824

1 + \frac{1}{12} = (1.0824)^{1/12}

1 + \frac{1}{12} = 1.00662

\frac{1}{12} = 0.00662

1 = 0.07944 = 7.94%

Thus, the two banks have different quoted rates—Bank A’s quoted rate is 8%, whereas Bank B’s quoted rate is 7.94%—yet both banks have the same effective annual rate of 8.24%. The difference in their quoted rates is due to the difference in compounding frequency.

**Chapter 5**

**ST-1**

a. Pennington’s bonds were sold at par; therefore, the original YTM equaled the coupon rate of 12%.

b. 

\[ V_B = \sum_{t=1}^{50} \frac{120/2}{1 + 0.10/2} + \frac{1,000}{1 + 1.10/2} \]

\[ = 60 \left[ \frac{1}{0.05} - \frac{1}{0.05(1 + 0.05)^{50}} \right] + \frac{1,000}{(1 + 0.05)^{50}} \]

\[ = 1,182.56 \]

Alternatively, with a financial calculator, input the following: \( N = 50, I/YR = 5, PMT = 60, \) and \( FV = 1000; \) solve for \( PV = -1,182.56. \)
c. Current yield = Annual coupon payment ÷ Price
   = $120/$1,182.56
   = 0.1015 = 10.15%
Capital gains yield = Total yield − Current yield
   = 10% − 10.15% = −0.15%
Total yield = Current yield + Capital gains yield
   = 10.15% + (−0.15%) = 10.00%

d. $916.42 = \sum_{t=1}^{13} \frac{$60}{(1 + r_d/2)^t} + \frac{$1000}{(1 + r_d/2)^{13}}

With a financial calculator, input the following: N = 13, PV = −916.42,
PMT = 60, and FV = 1000; then solve for r = I/YR = r_d/2 = 7.00%.
Therefore, r_d = 14.00%.
Current yield = $120/$916.42 = 13.09%
Capital gains yield = 14%−13.09% = 0.91%
Total yield = 14.00%

e. The following time line illustrates the years to maturity of the bond:

Thus, on March 1, 2010, there were 13^2/6 periods left before the bond
matured. Bond traders actually use the following procedure to determine the price of the bond.

(1) Find the price of the bond immediately after the next coupon is
paid on June 30, 2010:

   \[ V_B = \$60 \left[ \frac{1}{0.0775} - \frac{1}{0.0775(1 + 0.0775)^{13}} \right] + \frac{\$1,000}{(1 + 0.0775)^{13}} \]
   = $859.76

Using a financial calculator, input N = 13, I/YR = 7.75, PMT = 60,
and FV = 1000; then solve for PV = −$859.76.
(2) Add the coupon, $60, to the bond price to get the total value, TV,
of the bond on the next interest payment date: TV = $859.76 +
$60.00 = $919.76.
(3) Discount this total value back to the purchase date:

   \[ \text{Value at purchase date (March 1, 2010)} = \frac{$919.76}{(1 + 0.0775)^{4/6}} \]
   = $875.11

Using a financial calculator, input N = 4/6, I/YR = 7.75, PMT = 0,
and FV = 919.76; then solve for PV = $875.11.
(4) Therefore, you would have written a check for $875.11 to complete
the transaction. Of this amount, $20 = (\frac{1}{3})(\$60)$ would represent
accrued interest and $855.11 would represent the bond’s basic value. This breakdown would affect both your taxes and those of the seller.

(5) This problem could be solved very easily using a spreadsheet or a financial calculator with a bond valuation function.

CHAPTER 6

ST-1

a. The average rate of return for each stock is calculated simply by averaging the returns over the 5-year period. The average return for Stock A is

\[ r_{\text{Avg A}} = \frac{(-18\% + 44\% - 22\% + 22\% + 34\%)}{5} \]

\[ = 12\% \]

The realized rate of return on a portfolio made up of Stock A and Stock B would be calculated by finding the average return in each year as

\[ r_A(\% \text{ of Stock A}) + r_B(\% \text{ of Stock B}) \]

and then averaging these annual returns:

<table>
<thead>
<tr>
<th>Year</th>
<th>Portfolio AB's Return, ( r_{\text{AB}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2006</td>
<td>-21%</td>
</tr>
<tr>
<td>2007</td>
<td>34</td>
</tr>
<tr>
<td>2008</td>
<td>-13</td>
</tr>
<tr>
<td>2009</td>
<td>15</td>
</tr>
<tr>
<td>2010</td>
<td>45</td>
</tr>
</tbody>
</table>

\[ r_{\text{Avg}} = \frac{12\%}{5} \]

b. The standard deviation of returns is estimated as follows:

\[ \text{Estimated } \sigma = S = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (\bar{r}_i - \bar{r}_{\text{Avg}})^2} \]

For Stock A, the estimated \( \sigma \) is about 30%:

\[ \sigma_A = \sqrt{\frac{(-0.18 - 0.12)^2 + (0.44 - 0.12)^2 + (-0.22 - 0.12)^2 + (0.22 - 0.12)^2 + (0.34 - 0.12)^2}{5 - 1}} \]

\[ = 0.30265 \approx 30\% \]

The standard deviations of returns for Stock B and for the portfolio are similarly determined, and they are as follows:

<table>
<thead>
<tr>
<th>Stock A</th>
<th>Stock B</th>
<th>Portfolio AB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard deviation</td>
<td>30%</td>
<td>30%</td>
</tr>
</tbody>
</table>

c. Because the risk reduction from diversification is small (\( \sigma_{\text{AB}} \) falls only from 30% to 29%), the most likely value of the correlation coefficient is 0.8. If the correlation coefficient were -0.8, then the risk reduction would be much larger. In fact, the correlation coefficient between Stocks A and B is 0.8.

d. If more randomly selected stocks were added to a portfolio, \( \sigma_p \) would decline to somewhere in the vicinity of 20%. The value of \( \sigma_p \) would remain constant only if the correlation coefficient were +1.0, which is most unlikely. The value of \( \sigma_p \) would decline to zero only if (1) the correlation coefficient \( \rho \) were equal to zero and a large number of
The first step is to solve for $g$, the unknown variable, in the constant growth equation. Since $D_1$ is unknown but $D_0$ is known, substitute $D_0(1 + g)$ as follows:

$$\hat{P}_0 = P_0 = \frac{D_1}{r_s - g} = \frac{D_0(1 + g)}{r_s - g}$$

$\$36 = \frac{2.40(1 + g)}{0.12 - g}$.

Solving for $g$, we find the growth rate to be 5%:

$$4.32 - 36g = 2.40 + 2.40g$$
$$38.4g = 1.92$$
$$g = 0.05 = 5\%$$

The next step is to use the growth rate to project the stock price 5 years hence:

$$\hat{P}_5 = \frac{D_0(1 + g)^6}{r_s - g} = \frac{2.40(1.05)^6}{0.12 - 0.05} = \$45.95$$

(Alternatively, $\hat{P}_5 = 36(1.05)^5 = \$45.95$.) Therefore, Ewald Company's expected stock price 5 years from now, $P_5$, is $\$45.95$.

ST-2 a. (1) Calculate the PV of the dividends paid during the supernormal growth period:

$$D_1 = 1.1500(1.15) = 1.3225$$
$$D_2 = 1.1500(1.15) = 1.3225$$
$$D_3 = 1.3225(1.13) = 1.5209$$

$$PV\ of\ Div = \frac{1.3225}{1.12} + \frac{1.5209}{1.12^2} + \frac{1.7186}{1.12^3}$$
$$= \$3.6167 = \$3.62$$
(2) Find the PV of Snyder’s stock price at the end of Year 3:

\[ \hat{P}_3 = \frac{D_4}{r_s - g} = \frac{D_3(1 + g)}{r_s - g} \]

\[ = \frac{1.7186(1.06)}{0.12 - 0.06} = \frac{30.36}{\text{PV of } \hat{P}_3 = 30.36/(1.12)^3 = 21.61} \]

(3) Sum the two components to find the value of the stock today:

\[ \hat{P}_0 = 3.62 + 21.61 = 25.23 \]

Alternatively, the cash flows can be placed on a time line as follows:

\[ \begin{array}{cccccc}
0 & 1 & 2 & 3 & 4 \\
\text{g = 15%} & \text{g = 15%} & \text{g = 13%} & \text{g = 6%} \\
1.3225 & 1.5209 & 1.7186 & 1.8217 \\
\hline
\end{array} \]

\[ \frac{30.3617}{0.12 - 0.06} = \frac{1.8217}{32.0803} \]

Enter the cash flows into the cash flow register (CF0 = 0, CF1 = 1.3225, CF2 = 1.5209, CF3 = 32.0803) and I/YR = 12; then press the NPV key to obtain \( \hat{P}_0 = 25.23 \).

b. \( \hat{P}_1 = \frac{1.5209}{(1.12)} + \frac{1.7186}{(1.12)^2} + \frac{30.36}{(1.12)^3} \)

\[ = 26.9311 = 26.93 \]

(Calculator solution: 26.93.)

\( \hat{P}_2 = \frac{1.7186}{(1.12)} + \frac{30.36}{(1.12)} \)

\[ = 28.6429 = 28.64 \]

(Calculator solution: 28.64.)

c. \begin{array}{cccc}
\text{Year} & \text{Dividend Yield} & + & \text{Capital Gains Yield} & = & \text{Total Return} \\
1 & $1.3225 & = 5.24\% & + & $26.93 - $25.23 & = 6.74\% & = & 12\% \\
2 & $1.5209 & = 5.65\% & + & $28.64 - $26.93 & = 6.35\% & = & 12\% \\
3 & $1.7186 & = 6.00\% & + & $30.36 - $28.64 & = 6.00\% & = & 12\% \\
\end{array} \]

\[ \text{ST-1} \quad \text{The option will pay off } 60 - 42 = 18 \text{ if the stock price is up. The option pays off nothing (0) if the stock price is down. Find the number of shares in the hedge portfolio:} \]

\[ N = \frac{C_u - C_d}{P_u - P_d} = \frac{18 - 0}{60 - 30} = 0.60 \]
With 0.6 shares, the stock’s payoff will be either $0.6(60) = $36 or $0.6(30) = $18. The portfolio’s payoff will be $36 − $18 = $18, or $18 − 0 = $18.

The present value of $18 at the daily compounded risk-free rate is $18 / [1 + (0.05/365)]^{365} = $17.12. The option price is the current value of the stock in the portfolio minus the PV of the payoff:

\[ V = 0.6(40) - 17.12 = 6.88 \]

\[ d_1 = \frac{\ln(P/X) + [r_{RF} + (\sigma^2/2)]t}{\sigma\sqrt{t}} \]

\[ = \frac{\ln(22/20) + (0.05 + (0.49/2))(0.5)}{0.7\sqrt{0.5}} \]

\[ = 0.4906 \]

\[ d_2 = d_1 - \sigma(t)^{0.5} = 0.4906 - 0.7(0.5)^{0.5} = -0.0044 \]

\[ N(d_1) = 0.6881 \text{ (from Excel NORMSDIST function)} \]

\[ N(d_2) = 0.4982 \text{ (from Excel NORMSDIST function)} \]

\[ V = P[N(d_1)] - Xe^{-r_{RF}t}[N(d_2)] \]

\[ = 22(0.6881) - 20e^{-0.05(0.5)}(0.4982) \]

\[ = 5.42 \]

**Chapter 9**

**ST-1**

a. Component costs are as follows:

Debt at \( r_d = 9\% \):

\[ r_d(1 - T) = 9\%(0.6) = 5.4\% \]

Preferred with \( F = 5\% \):

\[ r_{ps} = \frac{\text{Preferred dividend}}{P_{ps}(1 - F)} = \frac{9}{100(0.95)} = 9.5\%. \]

Common with DCF:

\[ r_s = \frac{D_1}{P_0} + g = \frac{3.922}{60} + 6\% = 12.5\%. \]

Common with CAPM:

\[ r_s = 6\% + 1.3(5\%) = 12.5\% \]

b. WACC = \( w_d r_d(1 - T) + w_{ps} r_{ps} + w_s r_s \)

\[ = 0.25(9\%)(1 - T) + 0.15(9.5\%) + 0.60(12.5\%) \]

\[ = 10.275\% \]

**Chapter 10**

**ST-1**

a. Payback:

To determine the payback, construct the cumulative cash flows for each project as follows.
<table>
<thead>
<tr>
<th>Year</th>
<th>Project X</th>
<th>Project Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$-10,000</td>
<td>$-10,000</td>
</tr>
<tr>
<td>1</td>
<td>$-3,500</td>
<td>$-6,500</td>
</tr>
<tr>
<td>2</td>
<td>$-500</td>
<td>$-3,000</td>
</tr>
<tr>
<td>3</td>
<td>$2,500</td>
<td>$500</td>
</tr>
<tr>
<td>4</td>
<td>$3,500</td>
<td>$4,000</td>
</tr>
</tbody>
</table>

Payback_{X} = 2 + \frac{500}{3,000} = 2.17 \text{ years} \quad \text{Payback}_{Y} = 2 + \frac{3,000}{3,500} = 2.86 \text{ years}

**Net present value (NPV):**

\[
\begin{align*}
\text{NPV}_{X} &= -10,000 + \frac{6,500}{(1.12)^1} + \frac{3,000}{(1.12)^2} + \frac{3,000}{(1.12)^3} + \frac{1,000}{(1.12)^4} = $966.01 \\
\text{NPV}_{Y} &= -10,000 + \frac{3,500}{(1.12)^1} + \frac{3,500}{(1.12)^2} + \frac{3,500}{(1.12)^3} + \frac{3,500}{(1.12)^4} = $630.72
\end{align*}
\]

Alternatively, using a financial calculator, input the cash flows into the cash flow register, enter I/YR = 12, and then press the NPV key to obtain NPV_{X} = $966.01 and NPV_{Y} = $630.72.

**Internal rate of return (IRR):**

To solve for each project's IRR, find the discount rates that equate each NPV to zero:

IRR_{X} = 18.0\% \quad \text{IRR}_{Y} = 15.0\%

**Modified Internal Rate of Return (MIRR):**

To obtain each project's MIRR, begin by finding each project's terminal value (TV) of cash inflows:

\[
\begin{align*}
\text{TV}_{X} &= 6,500(1.12)^3 + 3,000(1.12)^2 + 3,000(1.12)^1 + 1,000 = $17,255.23 \\
\text{TV}_{Y} &= 3,500(1.12)^3 + 3,500(1.12)^2 + 3,500(1.12)^1 + 3,500 = $16,727.65
\end{align*}
\]

Now, each project's MIRR is the discount rate that equates the PV of the TV to each project's cost, $10,000:

MIRR_{X} = 14.61\% \quad \text{MIRR}_{Y} = 13.73\%

**Profitability index (PI):**

To obtain each project's PI, divide its present value of future cash flows by its initial cost. The PV of future cash flows can be found from the NPV calculated earlier:

\[
\begin{align*}
\text{PV}_{X} &= \text{NPV}_{X} + \text{Cost of X} = $966.01 + $10,000 = $10,966.01 \\
\text{PV}_{Y} &= \text{NPV}_{Y} + \text{Cost of Y} = $630.72 + $10,000 = $10,630.72 \\
\text{PI}_{X} &= \frac{\text{PV}_{X}}{\text{Cost of X}} = $10,966.01/$10,000 = 1.097 \\
\text{PI}_{Y} &= \frac{\text{PV}_{Y}}{\text{Cost of Y}} = $10,630.72/$10,000 = 1.063
\end{align*}
\]
b. The following table summarizes the project rankings by each method:

<table>
<thead>
<tr>
<th>Project That Ranks Higher</th>
<th>Payback</th>
<th>NPV</th>
<th>IRR</th>
<th>MIRR</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
<td>X</td>
</tr>
</tbody>
</table>

Note that all methods rank Project X over Project Y. Because both projects are acceptable under the NPV, IRR, and MIRR criteria, both should be accepted if they are independent.

c. In this case, we would choose the project with the higher NPV at $r = 12\%$, or Project X.

d. To determine the effects of changing the cost of capital, plot the NPV profiles of each project. The crossover rate occurs at about 6% to 7% (6.2%). See the graph below.

If the firm’s cost of capital is less than 6.2%, then a conflict exists because $\text{NPV}_Y > \text{NPV}_X$ but $\text{IRR}_X > \text{IRR}_Y$. Therefore, if $r$ were 5% then a conflict would exist. Note, however, that when $r = 5.0\%$ we have $\text{MIRR}_X = 10.64\%$ and $\text{MIRR}_Y = 10.83\%$; hence, the modified IRR ranks the projects correctly even if $r$ is to the left of the crossover point.

e. The basic cause of the conflict is differing reinvestment rate assumptions between NPV and IRR: NPV assumes that cash flows can be reinvested at the cost of capital, whereas IRR assumes that reinvestment yields the (generally) higher IRR. The high reinvestment rate assumption under IRR makes early cash flows especially valuable, so short-term projects look better under IRR.

NPV Profiles for Projects X and Y
### CHAPTER 11

#### ST-1

**a. Estimated Investment Requirements:**

<table>
<thead>
<tr>
<th></th>
<th>Price</th>
<th>Modification</th>
<th>Change in net working capital</th>
<th>Total investment</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Price</strong></td>
<td>−$50,000</td>
<td>−$10,000</td>
<td>−$2,000</td>
<td>−$62,000</td>
</tr>
</tbody>
</table>

**b. Operating Cash Flows:**

<table>
<thead>
<tr>
<th></th>
<th>Year 1</th>
<th>Year 2</th>
<th>Year 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. After-tax cost savings(^a)</td>
<td>$12,000</td>
<td>$12,000</td>
<td>$12,000</td>
</tr>
<tr>
<td>2. Depreciation(^b)</td>
<td>19,800</td>
<td>27,000</td>
<td>9,000</td>
</tr>
<tr>
<td>3. Depreciation tax savings(^c)</td>
<td>7,920</td>
<td>10,800</td>
<td>3,600</td>
</tr>
<tr>
<td>Operating cash flow ((1 + 3))</td>
<td>$19,920</td>
<td>$22,800</td>
<td>$15,600</td>
</tr>
</tbody>
</table>

\(^a\)$20,000\((1 - T)\).

\(^b\)Depreciable basis = $60,000; the MACRS percentage allowances are 0.33, 0.45, and 0.15 in Years 1, 2, and 3, respectively; hence, depreciation in Year 1 = 0.33($60,000) = $19,800, and so on. There will remain $4,200, or 7%, undepreciated after Year 3; it would normally be taken in Year 4.

\(^c\)Depreciation tax savings = \(T(\text{Depreciation}) = 0.4(19,800) = 7,920\) in Year 1, and so forth.

**c. Termination Cash Flow:**

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Salvage value</td>
<td>$20,000</td>
<td></td>
</tr>
<tr>
<td>Tax on salvage value(^a)</td>
<td>−$6,320</td>
<td></td>
</tr>
<tr>
<td>Net working capital recovery</td>
<td>2,000</td>
<td></td>
</tr>
<tr>
<td>Termination cash flow</td>
<td>$15,680</td>
<td></td>
</tr>
</tbody>
</table>

\(^a\)Calculation of tax on salvage value:

Book value = Depreciation basis − Accumulated depreciation

= $60,000 − $55,800 = $4,200

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Sales price</td>
<td>$20,000</td>
<td></td>
</tr>
<tr>
<td>Less book value</td>
<td>4,200</td>
<td></td>
</tr>
<tr>
<td>Taxable income</td>
<td>$15,800</td>
<td></td>
</tr>
<tr>
<td>Tax at 40%</td>
<td>$ 6,320</td>
<td></td>
</tr>
</tbody>
</table>
d. **Project NPV:**

<table>
<thead>
<tr>
<th>Year</th>
<th>Expected Cash Flows</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.2(−$100,000) + 0.6(−$100,000) + 0.2(−$100,000) = −$100,000</td>
</tr>
<tr>
<td>1</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>2</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>3</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>4</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>5</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>5*</td>
<td>0.2($0) + 0.6($20,000) + 0.2($30,000) = $ 18,000</td>
</tr>
</tbody>
</table>

Next, determine the NPV based on the expected cash flows:

\[
\text{NPV} = -100,000 + \frac{30,000}{(1.10)^1} + \frac{30,000}{(1.10)^2} + \frac{30,000}{(1.10)^3} + \frac{30,000}{(1.10)^4} + \frac{48,000}{(1.10)^5} = 24,900
\]

Alternatively, using a financial calculator, input the cash flows into the cash flow register, enter I/YR = 10, and then press the NPV key to obtain NPV = −$1,547. Because the earth mover has a negative NPV, it should not be purchased.

**ST-2**

a. First, find the expected cash flows:

<table>
<thead>
<tr>
<th>Year</th>
<th>Expected Cash Flows</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.2(−$100,000) + 0.6(−$100,000) + 0.2(−$100,000) = −$100,000</td>
</tr>
<tr>
<td>1</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>2</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>3</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>4</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>5</td>
<td>0.2($20,000) + 0.6($30,000) + 0.2($40,000) = $ 30,000</td>
</tr>
<tr>
<td>5*</td>
<td>0.2($0) + 0.6($20,000) + 0.2($30,000) = $ 18,000</td>
</tr>
</tbody>
</table>

Next, determine the NPV based on the expected cash flows:

\[
\text{NPV} = -100,000 + \frac{30,000}{(1.10)^1} + \frac{30,000}{(1.10)^2} + \frac{30,000}{(1.10)^3} + \frac{30,000}{(1.10)^4} + \frac{48,000}{(1.10)^5} = 24,900
\]

Alternatively, using a financial calculator, input the cash flows in the cash flow register, enter I/YR = 10, and then press the NPV key to obtain NPV = $24,900.

b. For the worst case, the cash flow values from the cash flow column farthest on the left are used to calculate NPV:

\[
\text{NPV} = -100,000 + \frac{20,000}{(1.10)^1} + \frac{20,000}{(1.10)^2} + \frac{20,000}{(1.10)^3} + \frac{20,000}{(1.10)^4} + \frac{20,000}{(1.10)^5} = -24,184
\]

Similarly, for the best case, use the values from the column farthest on the right. Here the NPV is $70,259.
If the cash flows are perfectly dependent, then the low cash flow in the first year will mean a low cash flow in every year. Thus, the probability of the worst case occurring is the probability of getting the $20,000 net cash flow in Year 1, or 20%. If the cash flows are independent, then the cash flow in each year can be low, high, or average and so the probability of getting all low cash flows will be

\[(0.2)(0.2)(0.2)(0.2)(0.2) = 0.2^5 = 0.0032 = 0.032\%\]

c. The base-case NPV is found using the most likely cash flows and is equal to $26,142. This value differs from the expected NPV of $24,900 because the Year-5 cash flows are not symmetric. Under these conditions, the NPV distribution is as follows:

<table>
<thead>
<tr>
<th>P</th>
<th>NPV</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>−$24,184</td>
</tr>
<tr>
<td>0.6</td>
<td>26,142</td>
</tr>
<tr>
<td>0.2</td>
<td>70,259</td>
</tr>
</tbody>
</table>

Thus, the expected NPV is 0.2(−$24,184) + 0.6($26,142) + 0.2($70,259) = $24,900. As is always the case, the expected NPV is the same as the NPV of the expected cash flows found in part a. The standard deviation is $29,904:

\[
\begin{align*}
\sigma_{NPV}^2 &= 0.2(-24,184 - 24,900)^2 + 0.6(26,142 - 24,900)^2 \\
&\quad + 0.2(70,259 - 24,900)^2 \\
&= 894,261,126 \\
\sigma_{NPV} &= \sqrt{894,261,126} = 29,904.
\end{align*}
\]

The coefficient of variation, CV, is $29,904/$24,900 = 1.20.

**ST-1**

To solve this problem, we first define \( \Delta S \) as the change in sales and \( g \) as the growth rate in sales. Then we use the three following equations:

\[
\Delta S = S_0g \\
S_1 = S_0(1 + g) \\
AFN = (A*/S_0)(\Delta S) - (L*/S_0)(\Delta S) - MS_1(1 - \text{Payout ratio})
\]

Set \( AFN = 0 \); substitute in known values for \( A*/S_0 \), \( L*/S_0 \), \( M \), \( d \), and \( S_0 \); and then solve for \( g \):

\[
0 = 1.6(100g) - 0.4(100g) - 0.10[100(1 + g)](0.55) \\
= 160g - 40g - 0.055(100 + 100g) \\
= 160g - 40g - 5.5 - 5.5g \\
$114.5g = 5.5 \\
g = 5.5/114.5 = 0.048 = 4.8\% \\
= \text{Maximum growth rate without external financing}
\]

**ST-2**

Assets consist of cash, marketable securities, receivables, inventories, and fixed assets. Therefore, we can break the \( A*/S_0 \) ratio into its components—cash/sales, inventories/sales, and so forth. Then,

\[
\frac{A^*}{S_0} = \frac{A^* - \text{Inventories}}{S_0} + \frac{\text{Inventories}}{S_0} = 1.6
\]
We know that the inventory turnover ratio is sales/inventories = 3 times, so inventories/sales = 1/3 = 0.3333. Further, if the inventory turnover ratio can be increased to 4 times, the inventory/sales ratio will fall to 1/4 = 0.25, a difference of 0.3333 − 0.2500 = 0.0833. This, in turn, causes the A*/S₀ ratio to fall from A*/S₀ = 1.6 to A*/S₀ = 1.6 − 0.0833 = 1.5167. This change has two effects: First, it changes the AFN equation; and second, it means that Barnsdale currently has excessive inventories. Because it is costly to hold excess inventories, Barnsdale will want to reduce its inventory holdings by not replacing inventories until the excess amounts have been used. We can account for this by setting up the revised AFN equation (using the new A*/S₀ ratio), estimating the funds that will be needed next year if no excess inventories are currently on hand, and then subtracting out the excess inventories that are currently on hand:

**Present Conditions:**

\[
\frac{\text{Sales}}{\text{Inventories}} = \frac{\$100}{\text{Inventories}} = 3
\]

so

\[
\text{Inventories} = \frac{\$100}{3} = \$33.3 \text{ million at present}
\]

**New Conditions:**

\[
\frac{\text{Sales}}{\text{Inventories}} = \frac{\$100}{\text{Inventories}} = 4
\]

so

\[
\text{New level of inventories} = \frac{\$100}{4} = \$25 \text{ million}
\]

Therefore,

\[
\text{Excess inventories} = \$33.3 - \$25 = \$8.3 \text{ million}
\]

**Forecast of Funds Needed, First Year:**

\[
\Delta S \text{ in first year} = 0.2(\$100 \text{ million}) = \$20 \text{ million}
\]

AFN = \(1.5167(\$20) - 0.4(\$20) - 0.1(0.55)(\$120) - \$8.3\)

\[= \$30.3 - \$8 - \$6.6 - \$8.3\]

\[= \$7.4 \text{ million}\]

**Forecast of Funds Needed, Second Year:**

\[
\Delta S \text{ in second year} = gS_1 = 0.2(\$120 \text{ million}) = \$24 \text{ million}
\]

AFN = \(1.5167(\$24) - 0.4(\$24) - 0.1(0.55)(\$144)\)

\[= \$36.4 - \$9.6 - \$7.9\]

\[= \$18.9 \text{ million}\]

ST-3

**a. Full capacity sales = \(\frac{\text{Current sales}}{\text{Percentage of capacity at which FA were operated}}\) = \(\frac{\$36,000}{0.75}\) = \$48,000**

**Percentage increase = \(\frac{\text{New sales} - \text{Old sales}}{\text{Old sales}}\) = \(\frac{\$48,000 - \$36,000}{\$36,000}\) = 0.33**

\[= 33\%\]
Therefore, sales could expand by 33% before Van Auken Lumber would need to add fixed assets.

b.

**Van Auken Lumber: Projected Income Statement for December 31, 2011**
(Thousands of Dollars)

<table>
<thead>
<tr>
<th></th>
<th>2010</th>
<th>FORECAST BASIS</th>
<th>2011</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sales</td>
<td>$36,000</td>
<td>1.25(Sales10)</td>
<td>$45,000</td>
</tr>
<tr>
<td>Operating costs</td>
<td>$30,783</td>
<td>85.508%(Sales11)</td>
<td>$38,479</td>
</tr>
<tr>
<td>EBIT</td>
<td>$5,217</td>
<td></td>
<td>$6,521</td>
</tr>
<tr>
<td>Interest</td>
<td>$717</td>
<td>12%(Debt10)</td>
<td>$1,017</td>
</tr>
<tr>
<td>EBT</td>
<td>$4,500</td>
<td></td>
<td>$5,504</td>
</tr>
<tr>
<td>Taxes (40%)</td>
<td>$1,800</td>
<td></td>
<td>$2,202</td>
</tr>
<tr>
<td>Net income</td>
<td>$2,700</td>
<td></td>
<td>$3,302</td>
</tr>
<tr>
<td>Dividends (60%)</td>
<td>$1,620</td>
<td></td>
<td>$1,981</td>
</tr>
<tr>
<td>Additions to RE</td>
<td>$1,080</td>
<td></td>
<td>$1,321</td>
</tr>
</tbody>
</table>

**Van Auken Lumber: Projected Balance Sheet for December 31, 2011**
(Thousands of Dollars)

<table>
<thead>
<tr>
<th></th>
<th>2010</th>
<th>PERCENT OF 2011 SALES ADDITIONS</th>
<th>2011</th>
<th>2011 AFTER AFN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cash</td>
<td>$1,800</td>
<td>5.000%</td>
<td>$2,250</td>
<td>$2,250</td>
</tr>
<tr>
<td>Receivables</td>
<td>10,800</td>
<td>30.000</td>
<td>13,500</td>
<td>13,500</td>
</tr>
<tr>
<td>Inventories</td>
<td>12,600</td>
<td>35.000</td>
<td>15,750</td>
<td>15,750</td>
</tr>
<tr>
<td>Total current assets</td>
<td>$25,200</td>
<td></td>
<td>$31,500</td>
<td>$31,500</td>
</tr>
<tr>
<td>Net fixed assets</td>
<td>$21,600</td>
<td></td>
<td>$21,600</td>
<td>$21,600</td>
</tr>
<tr>
<td>Total assets</td>
<td>$46,800</td>
<td></td>
<td>$53,100</td>
<td>$53,100</td>
</tr>
<tr>
<td>Accounts payable</td>
<td>$7,200</td>
<td>20.000</td>
<td>9,000</td>
<td>9,000</td>
</tr>
<tr>
<td>Notes payable</td>
<td>3,472</td>
<td></td>
<td>3,472</td>
<td>+2,549</td>
</tr>
<tr>
<td>Accruals</td>
<td>2,520</td>
<td>7.000</td>
<td>3,150</td>
<td>3,150</td>
</tr>
<tr>
<td>Total current liabilities</td>
<td>$13,192</td>
<td></td>
<td>$15,622</td>
<td>$18,171</td>
</tr>
<tr>
<td>Mortgage bonds</td>
<td>5,000</td>
<td></td>
<td>5,000</td>
<td>5,000</td>
</tr>
<tr>
<td>Common stock</td>
<td>2,000</td>
<td></td>
<td>2,000</td>
<td>2,000</td>
</tr>
<tr>
<td>Retained earnings</td>
<td>26,608</td>
<td>1,321b</td>
<td>27,929</td>
<td>27,929</td>
</tr>
<tr>
<td>Total liabilities and equity</td>
<td>$46,800</td>
<td></td>
<td>$50,551</td>
<td>$53,100</td>
</tr>
<tr>
<td>AFN</td>
<td></td>
<td></td>
<td>$2,549</td>
<td></td>
</tr>
</tbody>
</table>

aFrom part a we know that sales can increase by 33% before additions to fixed assets are needed.
bSee income statement

**CHAPTER 13**

ST-1 a.  \[ V_{op} = \frac{FCF(1 + g)}{WACC - g} = \frac{100,000(1 + 0.07)}{0.11 - 0.07} = $2,675,000 \]
b. Total value = Value of operations + Value of nonoperating assets  
   = $2,675,000 + $325,000 = $3,000,000  

c. Value of equity = Total value – Value of debt  
   = $3,000,000 – $1,000,000 = $2,000,000  

d. Price per share = Value of equity ÷ Number of shares  
   = $2,000,000 / 50,000 = $40

**Chapter 14**

**ST-1**  

a. Capital investments  
   Projected net income  
   Required equity = 40%(Capital inv.)  
   Available residual  
   Shares outstanding  

{\begin{align*}  
\text{DPS} &= \frac{\text{D}}{\text{EPS}} = \frac{2,600,000}{1,000,000} = 2.60  
\end{align*}}

b. EPS = $5,000,000 / 1,000,000 shares = 5.00  

Payout ratio = DPS/EPS = 2.6/5 = 52%, or  

Total dividends+NI = $2,600,000 / 5,000,000 = 52%

**Chapter 15**

**ST-1**  

a.  

{\begin{align*}  
S &= P(n) = \frac{30(600,000)}{600,000} = 18,000,000  
V &= D + S = 2,000,000 + 18,000,000 = 20,000,000  
\end{align*}}

b.  

{\begin{align*}  
wd &= D/V = \frac{2,000,000}{20,000,000} = 0.10  
w_s &= S/V = \frac{18,000,000}{20,000,000} = 0.90  
WACC &= w_d r_d (1 - T) + w_s r_s  
&= (0.10)(10\%)(0.60) + (0.90)(15\%) = 14.1\%  
\end{align*}}

c.  

{\begin{align*}  
WACC &= (0.50)(12\%)(0.60) + (0.50)(18\%) = 12.85\%  
\text{Since } g = 0, \text{ it follows that } FCF = NOPAT.  
\end{align*}}

{\begin{align*}  
V_{opNew} &= \frac{FCF}{WACC} = \frac{EBIT(1-T)}{WACC} = \frac{4,700,000(0.60)}{0.1285} = 21,945,525.292  
\end{align*}}

{\begin{align*}  
D &= w_d (V_{op}) = 0.50(21,945,525.292) = 10,972,762.646  
\end{align*}}

Since it started with $2 million debt, it will issue  

\(D_{New} - D_{Old} = 8,972,762.646 = 10,972,762.646 - 2,000,000.\)

\(S_{Post} = V_{opNew} - D_{New} = 21,945,525.292 - 10,972,762.646 = 10,972,762.646\)

(Alternatively,  

\(S_{Post} = w_s (V_{opNew}) = 0.50(21,945,525.292) = 10,972,762.646.\))

{\begin{align*}  
n_{Post} &= n_{Prior} = \frac{V_{opNew} - D_{New}}{V_{opNew} - D_{Old}}  
&= 600,000 \left[ \frac{21,945,525.292 - 10,972,762.646}{21,945,525.292 - 2,000,000} \right]  
&= 600,000 \left[ \frac{10,972,762.646}{19,945,525.292} \right]  
&= 330,082  
\end{align*}}
Alternatively, after issuing debt and before repurchasing stock, the firm’s equity, $S_{Prior}$, is worth $V_{opNew} + (D_{New} - D_{Old}) - D_{New} = 21,945,525.292 + 8,972,762.646 - 10,972,762.646 = 19,945,525.29. The stock price prior to the repurchase is $P_{Prior} = S_{Prior}/n_{Prior} = 19,945,525.29/600,000 = 33.242542. The firm used the proceeds of the new debt, $8,972,762.646, to repurchase $X$ shares of stock at a price of $33.242542 per share. The number of shares it will repurchase is $X = 8,972,762.646/33.242542 = 269,918.07$. Thus, there are $600,000 - 269,918.07 = 330,082$ shares remaining. As a check, the stock price should equal the market value of equity (S) divided by the number of shares: $P_0 = 10,972,762.646/330,082 = 33.2425$.

ST-2

a. LIC’s current cost of equity is

$$r_s = 6\% + 1.5(4\%) = 12\%$$

b. LIC’s unlevered beta is

$$b_U = 1.5/[1 + (1 - 0.40)(25\%/75\%)] = 1.5/1.2 = 1.25$$

c. LIC’s levered beta at D/S = 60%/40% = 1.5 is

$$b = 1.25[1 + (1 - 0.40)(60/40)] = 2.375$$

LIC’s new cost of capital will be

$$r_s = 6\% + (2.375)(4\%) = 15.5\%$$

### Chapter 16

ST-1 The Calgary Company: Alternative Balance Sheets

<table>
<thead>
<tr>
<th>Current assets (% of sales)</th>
<th>MODERATE (50%)</th>
<th>RELAXED (60%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$1,200,000</td>
<td>$1,800,000</td>
</tr>
<tr>
<td>Fixed assets</td>
<td>600,000</td>
<td>600,000</td>
</tr>
<tr>
<td>Total assets</td>
<td>$1,800,000</td>
<td>$2,100,000</td>
</tr>
<tr>
<td>Debt</td>
<td>$900,000</td>
<td>$1,050,000</td>
</tr>
<tr>
<td>Equity</td>
<td>900,000</td>
<td>1,050,000</td>
</tr>
<tr>
<td>Total liabilities and equity</td>
<td>$1,800,000</td>
<td>$2,100,000</td>
</tr>
</tbody>
</table>
The Calgary Company: Alternative Income Statements

<table>
<thead>
<tr>
<th></th>
<th>RESTRICTED</th>
<th>MODERATE</th>
<th>RELAXED</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sales</td>
<td>$3,000,000</td>
<td>$3,000,000</td>
<td>$3,000,000</td>
</tr>
<tr>
<td>EBIT</td>
<td>450,000</td>
<td>450,000</td>
<td>450,000</td>
</tr>
<tr>
<td>Interest (10%)</td>
<td>90,000</td>
<td>105,000</td>
<td>120,000</td>
</tr>
<tr>
<td>Earnings before taxes</td>
<td>$360,000</td>
<td>$345,000</td>
<td>$330,000</td>
</tr>
<tr>
<td>Taxes (40%)</td>
<td>144,000</td>
<td>138,000</td>
<td>132,000</td>
</tr>
<tr>
<td>Net income</td>
<td>$216,000</td>
<td>$207,000</td>
<td>$198,000</td>
</tr>
<tr>
<td>ROE</td>
<td>24.0%</td>
<td>19.7%</td>
<td>16.5%</td>
</tr>
</tbody>
</table>

Income Statements for Year Ended December 31, 2010 (Thousands of Dollars)

<table>
<thead>
<tr>
<th></th>
<th>VANDERHEIDEN PRESS</th>
<th>HERRENHOUSE PUBLISHING</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>a</td>
<td>b</td>
</tr>
<tr>
<td>EBIT</td>
<td>$30,000</td>
<td>$30,000</td>
</tr>
<tr>
<td>Interest</td>
<td>12,400</td>
<td>14,400</td>
</tr>
<tr>
<td>Taxable income</td>
<td>$17,600</td>
<td>$15,600</td>
</tr>
<tr>
<td>Taxes (40%)</td>
<td>7,040</td>
<td>6,240</td>
</tr>
<tr>
<td>Net income</td>
<td>$10,560</td>
<td>$9,360</td>
</tr>
<tr>
<td>Equity</td>
<td>$100,000</td>
<td>$100,000</td>
</tr>
<tr>
<td>Return on equity</td>
<td>10.56%</td>
<td>9.36%</td>
</tr>
</tbody>
</table>

The Vanderheiden Press has a higher ROE when short-term interest rates are high, whereas Herrenhouse Publishing does better when rates are lower.

c. Herrenhouse’s position is riskier. First, its profits and return on equity are much more volatile than Vanderheiden’s. Second, Herrenhouse must renew its large short-term loan every year, and if the renewal comes up at a time when money is tight or when its business is depressed or both, then Herrenhouse could be denied credit, which could put it out of business.

CHAPTER 17

ST-1

\[
\text{Euros} = \frac{\text{Euros}}{\text{US$}} \times \frac{\text{US$}}{\text{C$}}
\]

\[
= \frac{0.98}{0.6533} \times \frac{1}{1.5} = 0.98 = 0.6533 \text{ euros per Canadian dollar}
\]
Chapter 18

(ST-1) a. Cost of Leasing:

<table>
<thead>
<tr>
<th>YEAR 0</th>
<th>YEAR 1</th>
<th>YEAR 2</th>
<th>YEAR 3</th>
<th>YEAR 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lease payment</td>
<td>$-10,000</td>
<td>$-10,000</td>
<td>$-10,000</td>
<td>$-10,000</td>
</tr>
<tr>
<td>Payment tax savings</td>
<td>4,000</td>
<td>4,000</td>
<td>4,000</td>
<td>4,000</td>
</tr>
<tr>
<td>Net cash flow</td>
<td>$-6,000</td>
<td>$-6,000</td>
<td>$-6,000</td>
<td>$-6,000</td>
</tr>
<tr>
<td>PV cost of leasing @ 6% = $22,038</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

b. Cost of Owning:

In our solution, we will consider the $40,000 cost as a Year-0 outflow rather than including all the financing cash flows. The net effect is the same because the PV of the financing flows, when discounted at the after-tax cost of debt, is the cost of the asset.

<table>
<thead>
<tr>
<th>YEAR 0</th>
<th>YEAR 1</th>
<th>YEAR 2</th>
<th>YEAR 3</th>
<th>YEAR 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Net purchase price</td>
<td>$-40,000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Maintenance cost</td>
<td>$-1,000</td>
<td>$-1,000</td>
<td>$-1,000</td>
<td>$-1,000</td>
</tr>
<tr>
<td>Maintenance tax savings</td>
<td>400</td>
<td>400</td>
<td>400</td>
<td>400</td>
</tr>
<tr>
<td>Depreciation tax savings</td>
<td>5,280</td>
<td>7,200</td>
<td>2,400</td>
<td>1,120</td>
</tr>
<tr>
<td>Residual value</td>
<td></td>
<td>10,000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Residual value tax</td>
<td></td>
<td>4,000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Net cash flow</td>
<td>$-40,000</td>
<td>$4,680</td>
<td>$6,600</td>
<td>$1,800</td>
</tr>
<tr>
<td>PV cost of owning @ 6% = $23,035</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Since the present value of the cost of leasing is less than the present value of the cost of owning, the truck should be leased. Specifically, the NAL is $23,035 – $22,038 = $997.

c. Use the cost of debt because most cash flows are fixed by contract and thus are relatively certain; therefore, lease cash flows have about the same risk as the firm’s debt. Also, leasing is considered as a substitute for debt. Use an after-tax cost rate to account for interest tax deductibility.

Chapter 19

ST-1 First issue: 10-year straight bonds with a 6% coupon.

Second issue: 10-year bonds with 4.5% annual coupon with warrants. Both bonds issued at par $1,000. Value of warrants = ?

First issue: N = 10, PV = $-1000, PMT = 60, and FV = 1000; then solve for I/YR = r_d = 6% (Since it sold for par, we should know that r_d = 6%).

Second issue: $1,000 = Bond + Warrants. This bond should be evaluated at 6% (since we know the first issue sold at par) in order to determine its present value: N = 10, I/YR = r_d = 6, PMT = 45, and FV = 1000; then solve for PV = $889.60.

The value of the warrants can be determined as the difference between $1,000 and the second bond’s present value:

Value of warrants = $1,000 – $889.60 = $110.40.
CHAPTER 20

ST-1  a. Proceeds per share = \((1 - 0.07)($20) = $18.60.\) Required proceeds after direct costs: $30 million + $800,000 = $30.8 million.
Number of shares = $30.8 million/$18.60 per share = 1.656 million shares.

b. Amount left on table = \((\text{Closing price} - \text{offer price}) \times \text{Number of shares}\)
   = ($22 - $20)(1.656 million) = $3.312 million.

c. Underwriting cost = 0.07($20)(1.656) = $2.318 million.
Total costs = $0.800 + $2.318 + $3.312 = $6.430 million.

CHAPTER 21

ST-1  a. The unlevered cost of equity based on the pre-merger required rate of return and pre-merger capital structure is
   \[ r_{U} = w_d r_d + w_s r_s \]
   \[ = 0.25(6\%) + 0.75(10\%) \]
   \[ = 9\% \]

The post-horizon levered cost of equity is
   \[ r_{SL} = r_{U} + (r_{U} - r_d)(D/S) \]
   \[ = 9\% + (9\% - 7\%)(0.35/0.65) \]
   \[ = 10.077\% \]

WACC = \(w_d r_d (1 - T) + w_s r_s\)
   \[ = 0.35(7\%)(1 - 0.40) + 0.65(10.077\%) \]
   \[ = 8.02\% \]

b. The horizon value of unlevered operations is
   Horizon value \(HV_{U,3} = \frac{\text{FCF}_3(1 + g)}{r_{U} - g} \)
   \[ = \frac{[$25(1.05)]}{(0.09 - 0.05)} \]
   \[ = $656.250 \text{ million} \]

Unlevered \(V_{ops} = \frac{\$10}{(1.09)^1} + \frac{\$20}{(1.09)^2} + \frac{\$25 + $656.25}{(1.09)^3} \)
   \[ = $552.058 \text{ million} \]

Tax shields in Years 1 through 3 are
   Tax shield = Interest \times T
   \(TS_1 = $28.00(0.40) = $11.200 \text{ million} \)
   \(TS_2 = $24.00(0.40) = $9.600 \text{ million} \)
   \(TS_3 = $20.28(0.40) = $8.112 \text{ million} \)

Horizon value \(HV_{TS,3} = TS_3(1 + g)/(r_{U} - g) \)
   \[ = \frac{[$8.112(1.05)]}{(0.09 - 0.05)} \]
   \[ = $212.940 \text{ million} \]
Value of tax shield = \[ \frac{11.2}{(1.09)^1} + \frac{9.6}{(1.09)^2} + \frac{8.112 + 212.940}{(1.09)^3} \]

= $189.048 million

Total value = Unlevered V_{ops} + Value of tax shield
= $552.058 + $189.048
= $741.106.

**Chapter 22**

**ST-1**

a. Distribution to priority claimants (millions of dollars):

Total proceeds from the sale of assets $1,150
Less:
  1. First mortgage (paid from sale of fixed assets) 700
  2. Second mortgage (paid from sale of fixed assets after satisfying first mortgage: $750 – $700 = $50) 50
  3. Fees and expenses of bankruptcy 1
  4. Wages due to workers 60
  5. Taxes due 90
Funds available for distribution to general creditors $249

b. Distribution to general creditors (millions of dollars):

<table>
<thead>
<tr>
<th>GENERAL CREDITOR CLAIMS</th>
<th>AMOUNT OF CLAIM</th>
<th>PRO RATA DISTRIBUTION(^a)</th>
<th>DISTRIBUTION AFTER SUBORDINATE ADJUSTMENT(^b)</th>
<th>% OF ORIGINAL CLAIM RECEIVED</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unsatisfied second mortgage</td>
<td>$ 350</td>
<td>$ 60</td>
<td>$ 60</td>
<td>28(^c)</td>
</tr>
<tr>
<td>Accounts payable</td>
<td>100</td>
<td>17</td>
<td>17</td>
<td></td>
</tr>
<tr>
<td>Notes payable</td>
<td>300</td>
<td>52</td>
<td>86</td>
<td>29</td>
</tr>
<tr>
<td>Debentures</td>
<td>500</td>
<td>86</td>
<td>86</td>
<td>17</td>
</tr>
<tr>
<td>Subordinated debentures</td>
<td>200</td>
<td>34</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>$1,450</strong></td>
<td><strong>$249</strong></td>
<td><strong>$249</strong></td>
<td></td>
</tr>
</tbody>
</table>

Notes:
\(^a\)Pro rata distribution: $249/$1,450 = 0.172 = 17.2\%.
\(^b\)Subordinated debentures are subordinated to notes payable. Unsatisfied portion of notes payable is greater than subordinated debenture distribution, so subordinated debentures receive $0.
\(^c\)Includes $50 from sale of fixed assets received in priority distribution.

Total distribution to second mortgage holders: $50 + $60 = $110 million.
Total distribution to holders of notes payable: $86 million.
Total distribution to holders of subordinated debentures: $0 million.
Total distribution to common stockholders: $0 million.
CHAPTER 23

ST-1

a. The hypothetical bond in the futures contract has an annual coupon of 6% (paid semiannually) and a maturity of 20 years. At a price of 97’13 (this is the percent of par), a $1,000 par bond would have a price of $1,000(97 + 13/32)/100 = $974.0625. To find the yield: N = 40, PMT = 30, FV = 1000, PV = –974.0625; then I = 3.1143% per 6 months. The nominal annual yield is 2(3.1143%) = 6.2286%.

b. In this situation, the firm would be hurt if interest rates were to rise by September, so it would use a short hedge or sell futures contracts. Because futures contracts are for $100,000 in Treasury bonds, the value of a futures contract is $97,406.25 and the firm must sell $5,000,000/$97,406.25 = 51.33 ≈ 51 contracts to cover the planned $5,000,000 September bond issue. Because futures maturing in June are selling for 97 13/32 of par, the value of Wansley’s futures is about 51($97,406.25) = $4,967,718.75. Should interest rates rise by September, Wansley will be able to repurchase the futures contracts at a lower cost, which will help offset their loss from financing at the higher interest rate. Thus, the firm has hedged against rising interest rates.

c. The firm would now pay 13% on the bonds. With a 12% coupon rate, the PV of the new issue is only $4,646,361.83 (N = 40, I = 13/2 = 6.5, PMT = –0.12/2(500000) = –300000, FV = –500000; then solve for PV). Therefore, the new bond issue would bring in only $4,646,361.83, so the cost of the bond issue that is due to rising rates is $5,000,000 – $4,646,361.83 = $353,638.17. However, the value of the short futures position began at $4,967,718.75. Now, if interest rates increased by 1 percentage point, then the yield on the futures would go up to 7.2286% (7.2286 = 6.2286 + 1). To find the value of the futures contract, enter N = 40, I = 7.2286/2 = 3.6143 (from part a), PMT = 3000, and FV = 100000; then solve for PV = $87,111.04 per contract. With 51 contracts, the value of the futures position is $4,442,663.04. (Note: If you don’t round off in any previous calculations, then the PV comes to $4,442,668.38.)

Because Wansley Company sold the futures contracts for $4,967,718.75 and will, in effect, buy them back at $4,442,668.04, the firm would make a profit of $4,967,718.75 – $4,442,668.04 = $525,050.71 profit on the transaction (if we ignore transaction costs).

Thus, the firm gained $525,050.71 on its futures position, but lost $353,638.17 on its underlying bond issue. On net, it gained $525,050.71 – $353,638.17 = $171,412.54.

CHAPTER 24

ST-1

a. For Security A:

<table>
<thead>
<tr>
<th>PA</th>
<th>r_A</th>
<th>PA*r_A</th>
<th>(r_A - \hat{r}_A)</th>
<th>(r_A - \hat{r}_A)^2</th>
<th>PA(r_A - \hat{r}_A)^2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>-10%</td>
<td>-1.0%</td>
<td>-25%</td>
<td>625</td>
<td>62.5</td>
</tr>
<tr>
<td>0.2</td>
<td>5</td>
<td>1.0</td>
<td>-10</td>
<td>100</td>
<td>20.0</td>
</tr>
<tr>
<td>0.4</td>
<td>15</td>
<td>6.0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.2</td>
<td>25</td>
<td>5.0</td>
<td>10</td>
<td>100</td>
<td>20.0</td>
</tr>
<tr>
<td>0.1</td>
<td>40</td>
<td>4.0</td>
<td>25</td>
<td>625</td>
<td>62.5</td>
</tr>
</tbody>
</table>

\[ \hat{r}_A = 15.0\% \]

\[ \sigma_A = \sqrt{165.0} = 12.8\% \]
b. \[ w_A = \frac{\sigma_B (\sigma_B - \rho_{AB} \sigma_A)}{\sigma_A^2 + \sigma_B^2 - 2 \rho_{AB} \sigma_A \sigma_B} \]
\[ = \frac{25.7 [25.7 - (-0.5)(12.8)]}{(12.8)^2 + (25.7)^2 - 2(-0.5)(12.8)(25.7)} \]
\[ = \frac{824.97}{1,153.29} = 0.7153. \]
or 71.53% invested in A and 28.47% invested in B.

c. \[ \sigma_p = \sqrt{(w_A \sigma_A)^2 + (1-w_A)^2 (\sigma_B)^2 + 2w_A(1-w_A)\rho_{AB}\sigma_A \sigma_B} \]
\[ = \sqrt{(0.75)^2(12.8)^2 + (0.25)^2(25.7)^2 + 2(0.75)(0.25)(-0.5)(12.8)(25.7)} \]
\[ = \sqrt{92.16 + 41.28 - 61.68} \]
\[ = \sqrt{71.76} = 8.47\% \text{ when } w_A = 75\% \]
\[ \sigma_p = \sqrt{(0.153)^2(12.8)^2 + (0.2847)^2(25.7)^2 + 2(0.153)(0.2847)(-0.5)(12.8)(25.7)} \]
\[ = 8.38\% \text{ when } w_A = 71.53\% \text{ (this is the minimum } \sigma_p \text{)} \]
\[ \sigma_p = \sqrt{(0.5)^2(12.8)^2 + (0.5)^2(25.7)^2 + 2(0.5)(0.5)(-0.5)(12.8)(25.7)} \]
\[ = 11.3\% \text{ when } w_A = 50\% \]
\[ \sigma_p = \sqrt{(0.25)^2(12.8)^2 + (0.75)^2(25.7)^2 + 2(0.25)(0.75)(-0.5)(12.8)(25.7)} \]
\[ = 17.89\% \text{ when } w_A = 25\% \]

<table>
<thead>
<tr>
<th>% in A</th>
<th>% in B</th>
<th>( \hat{r}_p )</th>
<th>( \sigma_p )</th>
</tr>
</thead>
<tbody>
<tr>
<td>100%</td>
<td>0%</td>
<td>15.00%</td>
<td>12.8%</td>
</tr>
<tr>
<td>75</td>
<td>25</td>
<td>16.25</td>
<td>8.5</td>
</tr>
<tr>
<td>71.53</td>
<td>28.47</td>
<td>16.42</td>
<td>8.4</td>
</tr>
<tr>
<td>50</td>
<td>50</td>
<td>17.50</td>
<td>11.1</td>
</tr>
<tr>
<td>25</td>
<td>75</td>
<td>18.75</td>
<td>17.9</td>
</tr>
<tr>
<td>0</td>
<td>100</td>
<td>20.00</td>
<td>25.7</td>
</tr>
</tbody>
</table>

Calculations for preceding table:
\[ \hat{r}_p = w_A (\hat{r}_A) + (1 - w_A) (\hat{r}_B) \]
\[ = 0.75(15) + (0.25)(20) = 16.25\% \text{ when } w_A = 75\% \]
\[ = 0.7153(15) + 0.2847(20) = 16.42\% \text{ when } w_{A0} = 71.53\% \]
\[ = 0.5(15) + 0.5(20) = 17.50\% \text{ when } w_A = 50\% \]
\[ = 0.25(15) + 0.75(20) = 18.75\% \text{ when } w_A = 25\% \]
d. See graph below.

\[ \hat{r}_p = w_A \hat{r}_A + (1 - w_A) \hat{r}_B \]
\[ 18 = w_A (15) + (1 - w_A)(20) \]
\[ = 15w_A + 20 - 20w_A \]
\[ 5w_A = 2 \]
\[ w_A = 0.4 \text{ or } 40\% \]

Therefore, to an approximation, your optimal portfolio would have 40% in A and 60% in B, with \( \hat{r}_p = 18\% \) and \( \sigma_p = 13.5\% \). (We could get an exact \( \sigma_p \) by using \( w_A = 0.4 \) in the equation for \( \sigma_p \).)

e. See indifference curve IC1 in the preceding graph. At the point where \( \hat{r}_p = 18\% \), \( \sigma_p = 13.5\% \).

f. The existence of the riskless asset would enable you to go to the CAPM. We would draw in the CML as shown on the graph in part d. Now you would hold a portfolio of stocks, borrowing on margin to hold more stocks than your net worth, and move to a higher indifference curve, IC2.

You can put all of your money into the riskless asset, all in A, all in B, or some in each security. The most logical choices are (1) hold a portfolio of A and B plus some of the riskless asset, (2) hold only a portfolio of A and B, or (3) hold a portfolio of A and B and borrow to leverage the portfolio, assuming you can borrow at the riskless rate.

Reading from the graph, we see that your \( \hat{r}_p \) at the point of tangency between your IC2 and the CML is about 22%. We can use this information to find out how much you invest in the market portfolio and how much you invest in the riskless asset. (It will turn out that you have a negative investment in the riskless asset, which means that you borrow rather than lend at the risk-free rate.)
\[
\hat{r}_p = w_{RF}(r_{RF}) + (1 - w_{RF})(\hat{r}_M) \\
22 = w_{RF}(10) + (1 - w_{RF})(16.8) \\
-6.8w_{RF} = 5.2 \\
w_{RF} = -0.76 \text{ or } -76\% \text{ (which means that you borrow)} \\
1 - w_{RF} = 1.0 - (-0.76) \\
= +1.76 \text{ or } 176\% \text{ in the market portfolio}
\]
Hence this investor, with $200,000 of net worth, buys stock with a value of $200,000(1.76) = $352,000 and borrows $152,000.

The risk of this leveraged portfolio is
\[
\sigma_p = \sqrt{(-0.76)^2(0)^2 + (1.76)^2(8.5)^2 + 2(-0.76)(1.76)(0)(8.5)(0)} \\
= \sqrt{(1.76)^2(8.5)^2} \\
= (1.76)(8.5) = 15\%
\]
Your indifference curve suggests that you are not very risk averse. A risk-averse investor would have a steep indifference curve (visualize a set of steep curves that were tangent to CML to the left of Point C). This investor would hold some of A and B, combined to form portfolio M, and some of the riskless asset.

g. Given your assumed indifference curve, you would, when the riskless asset becomes available, change your portfolio from the one found in part e (with \( \hat{r}_p = 18\% \) and \( \sigma_p = 13.5\% \)) to one with \( \hat{r}_p = 22.0\% \) and \( \sigma_p = 15.00\% \).

h. \[r_A = r_{RF} + (r_M - r_{RF})b_A\] 
\[15 = 10 + (16.8 - 10)b_A\] 
\[= 10 + (6.8)b_A.\] 
\[b_A = 0.74.\] 
\[20 = 10 + (6.8)b_B\] 
\[b_B = 1.47\]
Note that the 16.8\% value for \( r_M \) was approximated from the graph. Also, this solution assumes that you can borrow at \( r_{RF} = 10\% \). This is a basic—but questionable—CAPM assumption. If the borrowing rate is above \( r_{RF} \), then the CML would turn down to the right of Point M.

**Chapter 25**

**ST-1**

a. NPV of each demand scenario:

<table>
<thead>
<tr>
<th>Probability</th>
<th>Future Cash Flows</th>
<th>NPV This Scenario</th>
<th>Probability × NPV</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>25%</td>
<td>$13 $13</td>
<td>$13.13</td>
<td>$3.28</td>
</tr>
<tr>
<td>$13 $13</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>25%</td>
<td>$7 $7</td>
<td>$3.38</td>
<td>$1.69</td>
</tr>
<tr>
<td>$7 $7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>50%</td>
<td>$1 $1</td>
<td>$6.37</td>
<td>$1.59</td>
</tr>
<tr>
<td>$1 $1</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Expected NPV of future CFs = $3.38
NPV under high-demand scenario:

\[ \text{NPV} = -8 + \frac{13}{(1 + 0.15)^1} + \frac{13}{(1 + 0.15)^2} = 13.13 \]

NPV under medium-demand scenario:

\[ \text{NPV} = -8 + \frac{7}{(1 + 0.15)^1} + \frac{7}{(1 + 0.15)^2} = 3.38 \]

NPV under low-demand scenario:

\[ \text{NPV} = -8 + \frac{1}{(1 + 0.15)^1} + \frac{1}{(1 + 0.15)^2} = -6.37 \]

Expected NPV = 0.25($13.13) + 0.50($3.38) + 0.25($6.37) = $3.38 million.

b. NPV of operating cash flows if the additional project is implemented only when optimal:

<table>
<thead>
<tr>
<th>Probability</th>
<th>Year 1</th>
<th>Year 2</th>
<th>Year 3</th>
<th>Year 4</th>
<th>NPV This Scenario</th>
<th>Probability \times NPV</th>
</tr>
</thead>
<tbody>
<tr>
<td>25%</td>
<td>$13</td>
<td>$13</td>
<td>$13</td>
<td>$13</td>
<td>$37.11</td>
<td>$9.28</td>
</tr>
<tr>
<td>50%</td>
<td>$7</td>
<td>$7</td>
<td>$7</td>
<td>$7</td>
<td>$19.98</td>
<td>$9.99</td>
</tr>
<tr>
<td>25%</td>
<td>$1</td>
<td>$1</td>
<td>$0</td>
<td>$0</td>
<td>$1.63</td>
<td>$0.41</td>
</tr>
</tbody>
</table>

Expected NPV of future operating CFs = $19.68 million

NPV of operating cash flows under high-demand scenario:

\[ \text{NPV} = \frac{13}{(1 + 0.15)^1} + \frac{13}{(1 + 0.15)^2} + \frac{13}{(1 + 0.15)^3} + \frac{13}{(1 + 0.15)^4} = 37.11 \]

NPV of operating cash flows under medium-demand scenario:

\[ \text{NPV} = \frac{7}{(1 + 0.15)^1} + \frac{7}{(1 + 0.15)^2} + \frac{7}{(1 + 0.15)^3} + \frac{7}{(1 + 0.15)^4} = 19.98 \]

NPV of operating cash flows under low-demand scenario:

\[ \text{NPV} = \frac{1}{(1 + 0.15)^1} + \frac{1}{(1 + 0.15)^2} = 1.63 \]

Expected NPV of operating cash flows = 0.25($37.11) + 0.50($19.98) + 0.25($1.63) = $19.68 million

Find NPV of costs, discounted at risk-free rate:
NPV of costs under high-demand scenario:

\[
NPV = -8 + \frac{0}{(1 + 0.06)^1} + \frac{-8}{(1 + 0.06)^2} = -15.12
\]

NPV of costs under medium-demand scenario:

\[
NPV = -8 + \frac{0}{(1 + 0.06)^1} + \frac{-8}{(1 + 0.06)^2} = -15.12
\]

NPV of costs under low-demand scenario:

\[
NPV = -8 + \frac{0}{(1 + 0.06)^1} + \frac{0}{(1 + 0.06)^2} = -8.00
\]

Expected NPV of costs = \(0.25(-15.12) + 0.50(-15.12) + 0.25(-8.00)\) = \(-13.34\) million

Expected NPV of future operating CFs = \(-13.34\) million

c. Find the expected NPV of the additional project’s operating cash flows, which is analogous to the “stock price” in the Black-Scholes model:

Future Operating Cash Flows of Additional Project (Discount at WACC)

<table>
<thead>
<tr>
<th>Year 1</th>
<th>Year 2</th>
<th>Year 3</th>
<th>Year 4</th>
<th>NPV of This Scenario</th>
</tr>
</thead>
<tbody>
<tr>
<td>$0</td>
<td>$0</td>
<td>$13</td>
<td>$13</td>
<td>$15.98</td>
</tr>
<tr>
<td>$8</td>
<td>$0</td>
<td>$7</td>
<td>$7</td>
<td>$8.60</td>
</tr>
<tr>
<td>$0</td>
<td>$0</td>
<td>$1</td>
<td>$1</td>
<td>$1.23</td>
</tr>
</tbody>
</table>

Expected NPV future operating CFs = \$8.60
NPV of operating cash flows under high-demand scenario:
$$\text{NPV} = \frac{0}{(1 + 0.15)^1} + \frac{0}{(1 + 0.15)^2} + \frac{13}{(1 + 0.15)^3} + \frac{13}{(1 + 0.15)^4} = $15.98$$

NPV of operating cash flows under medium-demand scenario:
$$\text{NPV} = \frac{0}{(1 + 0.15)^1} + \frac{0}{(1 + 0.15)^2} + \frac{7}{(1 + 0.15)^3} + \frac{7}{(1 + 0.15)^4} = $8.60$$

NPV of operating cash flows under low-demand scenario:
$$\text{NPV} = \frac{0}{(1 + 0.15)^1} + \frac{0}{(1 + 0.15)^2} + \frac{1}{(1 + 0.15)^3} + \frac{1}{(1 + 0.15)^4} = $1.23$$

Expected NPV of additional project’s operating cash flows:
$$= 0.25(15.98) + 0.50(8.60) + 0.25(1.23) = $8.60 \text{ million}$$

The inputs for the Black-Scholes model are: \( r_{RF} = 0.06, X = 8, P = 8.6 \), \( t = 2 \), and \( \sigma^2 = 0.150 \). Using these inputs, the value of the option, \( V \), is

$$d_1 = \frac{\ln(P/X) + \left[ r_{RF} + \frac{\sigma^2}{2} \right] \times t}{\sigma \sqrt{t}} = \frac{\ln(8.6/8) + \left[ 0.06 + \frac{0.150}{2} \right] \times 2}{\sqrt{0.15 \times 2}} = 0.62499$$

$$d_2 = d_1 - \sigma \sqrt{t} = 0.62499 - \sqrt{0.15 \times 2} = 0.07727$$

Use Excel’s NORMSDIST function to calculate \( N(d_1) \) and \( N(d_2) \):

\( N(d_1) = 0.73401 \)
\( N(d_2) = 0.53079 \)

\( V = P[N(d_1)] - X e^{-r_{RF}t}[N(d_2)] = 8.6(0.73401) - 8 e^{-0.06(2)}(0.53079) = $2.55 \text{ million} \)

The total value is the value of the original project (from part a) and the value of the growth option:

Total value = $3.38 + $2.55 = $5.93 million

**Chapter 26**

**ST-1**

a. Value of unleveraged firm, \( V_U = EBIT(1 - T)/r_{SU} \):

\[ \begin{align*}
$12 &= 2(1-0.4)r_{SU} \\
$12 &= 1.2/r_{SU} \\
r_{SU} &= 1.2/12 = 10.0\% \\
\end{align*} \]

Therefore, \( r_{SU} = \text{WACC} = 10.0\% \).

b. Value of leveraged firm according to MM mode with taxes:

\[ V_L = V_U + TD \]
As shown in the following table, value increases continuously with debt, and the optimal capital structure consists of 100% debt. Note: The table is not necessary to answer this question, but the data (in millions of dollars) are necessary for part c of the problem.

<table>
<thead>
<tr>
<th>DEBT, D</th>
<th>V_U</th>
<th>TD</th>
<th>V_L = V_U + TD</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>12.0</td>
<td>0.0</td>
<td>12.0</td>
</tr>
<tr>
<td>2.5</td>
<td>12.0</td>
<td>1.0</td>
<td>13.0</td>
</tr>
<tr>
<td>5.0</td>
<td>12.0</td>
<td>2.0</td>
<td>14.0</td>
</tr>
<tr>
<td>7.5</td>
<td>12.0</td>
<td>3.0</td>
<td>15.0</td>
</tr>
<tr>
<td>10.0</td>
<td>12.0</td>
<td>4.0</td>
<td>16.0</td>
</tr>
<tr>
<td>12.5</td>
<td>12.0</td>
<td>5.0</td>
<td>17.0</td>
</tr>
<tr>
<td>15.0</td>
<td>12.0</td>
<td>6.0</td>
<td>18.0</td>
</tr>
<tr>
<td>20.0</td>
<td>12.0</td>
<td>8.0</td>
<td>20.0</td>
</tr>
</tbody>
</table>

c. With financial distress costs included in the analysis, the value of the leveraged firm is now

\[ V_L = V_U + TD - PC \]

where

\[ V_U + TD = \text{Value according to MM after-tax model}. \]
\[ P = \text{Probability of financial distress}. \]
\[ C = \text{Present value of distress costs}. \]

<table>
<thead>
<tr>
<th>D</th>
<th>V_U + TD</th>
<th>P</th>
<th>PC = (P)$8</th>
<th>V_L = V_U + TD − PC</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>12.0</td>
<td>0.0000</td>
<td>0.00</td>
<td>12.0</td>
</tr>
<tr>
<td>2.5</td>
<td>13.0</td>
<td>0.0000</td>
<td>0.00</td>
<td>13.0</td>
</tr>
<tr>
<td>5.0</td>
<td>14.0</td>
<td>0.0125</td>
<td>0.10</td>
<td>13.9</td>
</tr>
<tr>
<td>7.5</td>
<td>15.0</td>
<td>0.0250</td>
<td>0.20</td>
<td>14.8</td>
</tr>
<tr>
<td>10.0</td>
<td>16.0</td>
<td>0.0625</td>
<td>0.50</td>
<td>15.5</td>
</tr>
<tr>
<td>12.5</td>
<td>17.0</td>
<td>0.1250</td>
<td>1.00</td>
<td>16.0</td>
</tr>
<tr>
<td>15.0</td>
<td>18.0</td>
<td>0.3125</td>
<td>2.50</td>
<td>15.5</td>
</tr>
<tr>
<td>20.0</td>
<td>20.0</td>
<td>0.7500</td>
<td>6.00</td>
<td>14.0</td>
</tr>
</tbody>
</table>

Note: All dollar amounts are in millions.

Optimal debt level: D = $12.5 million.
Maximum value of firm: V = $16.0 million.
Optimal debt/value ratio: D/V = $12.5/$16 = 78%.
d. The value of the firm versus debt value with and without financial distress costs is plotted next (millions of dollars), where

\[ V_L = \text{Value without financial distress costs.} \]
\[ V_B = \text{Value with financial distress costs.} \]